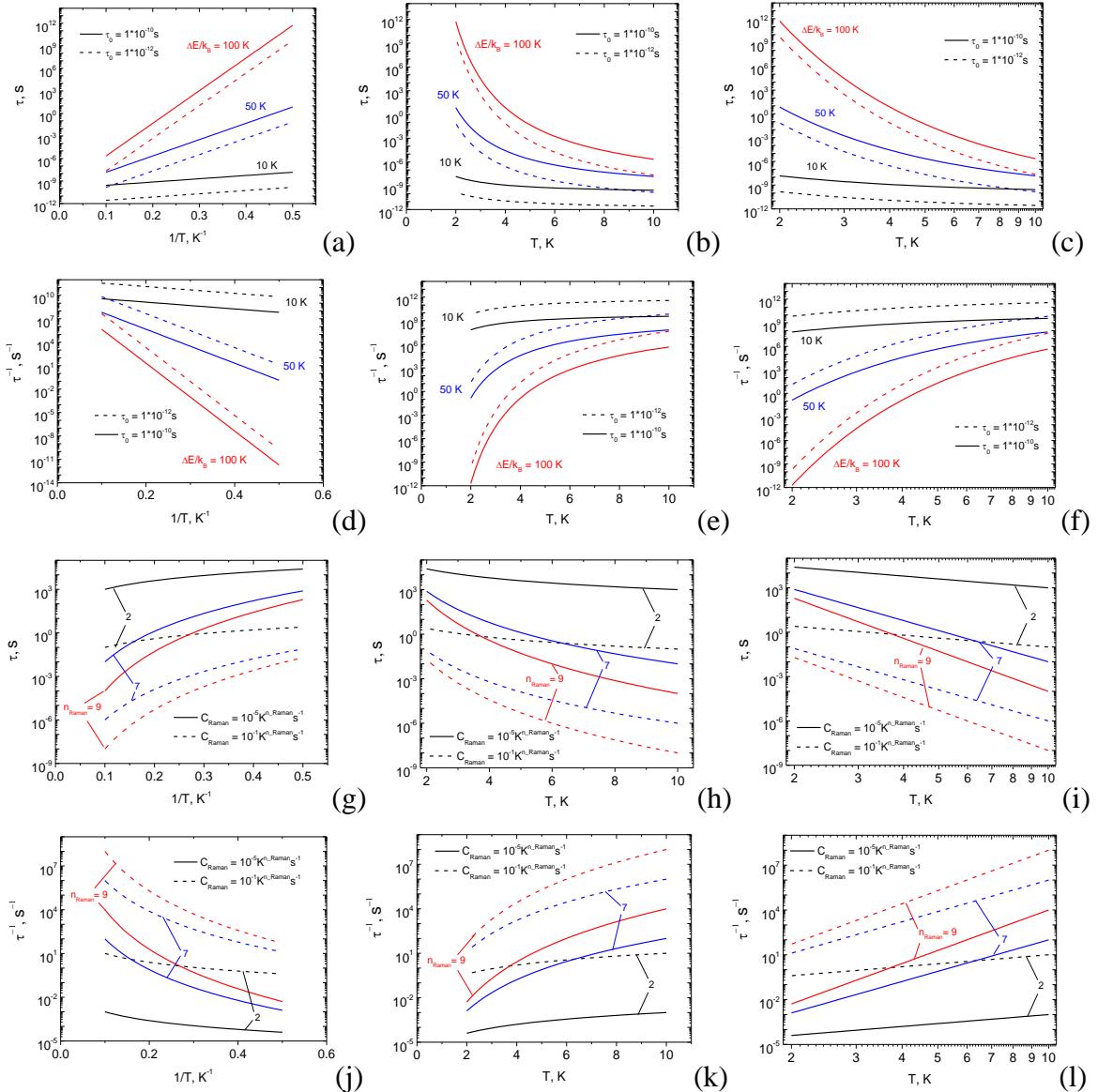


# МЕТОД ДИНАМИЧЕСКОЙ МАГНИТНОЙ ВОСПРИИМЧИВОСТИ В ИССЛЕДОВАНИИ КООРДИНАЦИОННЫХ СОЕДИНЕНИЙ

© 2024 г. Н. Н. Ефимов<sup>1</sup>, \*, К. А. Бабешкин<sup>1</sup>, А. В. Ротов<sup>1</sup>

<sup>1</sup>Институт общей и неорганической химии им. Н.С. Курнакова РАН, Москва, Россия

\*e-mail: nnefimov@narod.ru



**Fig. S1.** Dependences of relaxation time( $\tau$ ) vs. temperature (T) for different versions of coordinate axes for the Orbach (a-f) and Raman (g-l) mechanisms with the parameters presented on the graphs.

## **View of the generalized Debye model in the Origin program.**

Part of the \*.fdf file (Origin program) with the formula for approximating the dependence  $\chi'(v)$  by the generalized Debye model.

[Fitting Parameters]

Names = Hi\_inf,dHi,Tau,Alpha

[Independent Variables]

v =

[Dependent Variables]

Hi1 =

[Formula]

Hi\_inf+((dHi)\*(1+(2\*Pi\*v\*Tau)^(1-Alpha)\*sin(0.5\*Alpha\*3.1416)))/(1+2\*(2\*Pi\*v\*Tau)^(1-Alpha)\*sin(0.5\*Alpha\*3.1416)+(2\*Pi\*v\*Tau)^(2-2\*Alpha))

Part of the \*.fdf file (Origin program) with the formula for approximating the dependence  $\chi''(v)$  by the generalized Debye model.

[Fitting Parameters]

Names = dHi,Tau,Alpha

[Independent Variables]

v =

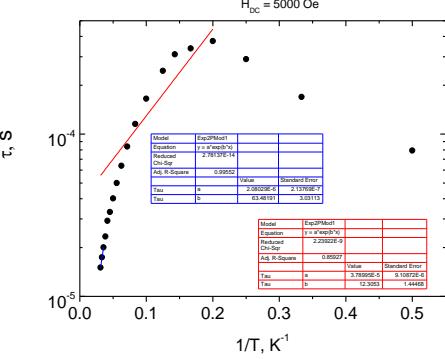
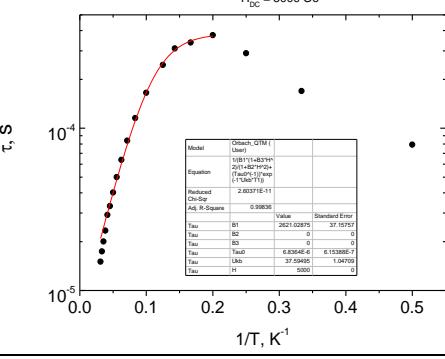
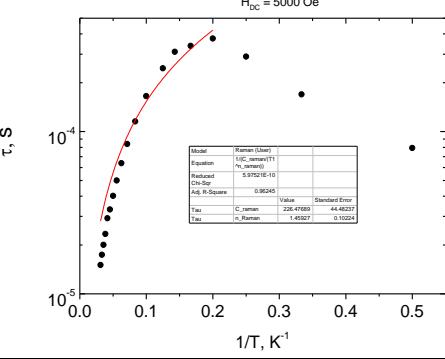
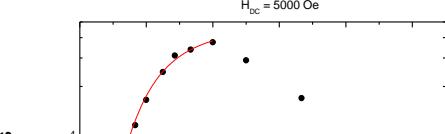
[Dependent Variables]

Hi2 =

[Formula]

((dHi)\*(2\*Pi\*v\*Tau)^(1-Alpha)\*cos(0.5\*Alpha\*3.1416))/(1+2\*(2\*Pi\*v\*Tau)^(1-Alpha)\*sin(0.5\*Alpha\*3.1416)+(2\*Pi\*v\*Tau)^(2-2\*Alpha))

**Table S1.** An example of enumerating relaxation mechanisms when interpreting measurement data for a complex **1** -  $[\text{NaGd}(\text{VO})_2(\text{cbdc})_4(\text{H}_2\text{O})_{10}]_n$ , where cbdc - cyclobutane-1,1-dicarboxylic acid anion. [Bazhina E.S., Korlyukov A.A., Voronina J.K. et al. // Magnetochemistry. 2021. V. 7]

Dependence of the relaxation time $\tau$ on the reciprocal temperature for complex <b>1</b> ( $H = 5$ kOe, $T = 6\text{--}32$ K).	Fit function, temperature range, and the best-fit parameters with uncertainties.																																		
 <table border="1" data-bbox="277 808 722 871"> <tr><td>Model</td><td>Orbach (User)</td></tr> <tr><td>Equation</td><td><math>y = x \cdot \exp(-E/kT)</math></td></tr> <tr><td>Reduced Chi-Sqr</td><td>2.052052</td></tr> <tr><td>Adj. R-Square</td><td>0.99552</td></tr> <tr><td>Tau</td><td><math>\tau_0 = 2.052052 \cdot 10^{-6}</math> Value: 2.052052 Standard Error: 0.000000</td></tr> <tr><td>Tau</td><td><math>n = 13.43051 \cdot 10^{-5}</math> Value: 13.43051 Standard Error: 0.000013</td></tr> </table> <table border="1" data-bbox="277 871 722 934"> <tr><td>Model</td><td>Orbach+QTM</td></tr> <tr><td>Equation</td><td><math>y = x^{\alpha} \cdot \exp(-E/kT) + B</math></td></tr> <tr><td>Reduced Chi-Sqr</td><td>2.05927</td></tr> <tr><td>Adj. R-Square</td><td>0.85927</td></tr> <tr><td>Tau</td><td><math>\tau_0 = 3.795956 \cdot 10^{-5}</math> Value: 3.795956 Standard Error: 0.103725</td></tr> <tr><td>Tau</td><td><math>B = 12.3051 \cdot 10^{-5}</math> Value: 12.3051 Standard Error: 1.44468</td></tr> </table>	Model	Orbach (User)	Equation	$y = x \cdot \exp(-E/kT)$	Reduced Chi-Sqr	2.052052	Adj. R-Square	0.99552	Tau	$\tau_0 = 2.052052 \cdot 10^{-6}$ Value: 2.052052 Standard Error: 0.000000	Tau	$n = 13.43051 \cdot 10^{-5}$ Value: 13.43051 Standard Error: 0.000013	Model	Orbach+QTM	Equation	$y = x^{\alpha} \cdot \exp(-E/kT) + B$	Reduced Chi-Sqr	2.05927	Adj. R-Square	0.85927	Tau	$\tau_0 = 3.795956 \cdot 10^{-5}$ Value: 3.795956 Standard Error: 0.103725	Tau	$B = 12.3051 \cdot 10^{-5}$ Value: 12.3051 Standard Error: 1.44468	<b>Orbach</b> $\tau = \tau_0 \cdot \exp(-E/kT)$ $T = 28\text{--}32$ K $E/k = 63 \pm 3$ K $\tau_0 = 2.1 \cdot 10^{-6} \pm 2 \cdot 10^{-7}$ s $R^2 = 0.99552$ (blue line)  $T = 6\text{--}32$ K $E/k = 12 \pm 1$ K $\tau_0 = 3.8 \cdot 10^{-5} \pm 9 \cdot 10^{-6}$ s $R^2 = 0.85927$ (red line) <i>Unsatisfactory fit</i>										
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